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Optimization of adaptive neuro fuzzy inference system based urban growth model

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Abstract

Background: Global urban population has increased from 22.9 % in 1985 to 47 % in 2010. In Iran, population living in urban areas has consistently increased from about 31 % in 1956 to 68.4 % in 2006. Urban growth as one of the results of rapid population growth, results lots of problems. Thus, monitoring and modelling of the urban expansion is necessary.

Methods: In this research, a novel Adaptive Neuro Fuzzy Inference System (ANFIS)-based methodology has been developed for urban growth modeling, as well as interpreting the relationship between the drivers of urbanization. Then, ANFIS results were compared with those achieved by both ANN and Logistic Regression (LR)-based methodologies using Percent Area Match quantity and Percent Area Match location to assess model goodness of fit.

Results: The proposed ANFIS model which takes the advantages of using neural networks and fuzzy logic at the same time, had the best performances among the three implemented models. It was able to identify important factors in the development and their relationship and influence on the growth of the city.

Conclusions: The research aim is to find a computational based method which can effectively capture, analyse and model the complex nature of spatial phenomenon like urban growth. The proposed ANFIS method due to its structure is able to deals with nonlinear phenomenon. Integration of Remote sensing data, GIS tools and also, computational based method provide us an effective, reliable and also, scientific methods for monitoring, analysing and modeling of environmental phenomenon.

Keywords: Urban growth, Modeling, ANFIS

Background

Unprecedented population growth in the cities has caused a number of problems such as improper planning of infrastructure and urban services, environmental pollution and human health problems. Urban growth as one of its results has created many environmental and socioeconomic problems during the last decades (Triantakou et al. 2012). In fact, urban growth can be considered as the transformation of the rural areas to cities and towns, which is coming along with costs (Deep and Saklani 2014). Urban growth as a complex system is affected by human and non-human based parameters. Spatio-temporal dynamics and incorporation of human drivers

of land use changes have the most important impact on land use change (Veldkamp and Lambin 2001). Recognition of effective natural, social and spatiotemporal processes that affect urban growth can enhance the accuracy and reliability of the proposed modeling procedure (Foroutan et al. 2012).

Nowadays, due to the high value of land and natural resources and land use change affecting ecosystems and humans, land use change modeling is very important for the concerned urban executives, professionals and researchers. The aim of using urban growth model is to achieve two goals. First, implementation of techniques to understand the spatial relationship between urban growth driving factors (or proxies for them) and historical changes in urban land use. Second, projection of spatial changes in land use based on scenarios of changes in its drivers (Meiyappan et al. 2014). With analyzing

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historical spatiotemporal information, nature of spatiotemporal dynamics of land use changes resulted from different land use policies can be understood which can serve as a basis for developing possible growth scenarios essential for sustainable urban planning and development (Tayyebi et al. 2011).

Recently, a large number of urban expansion models have been implemented in so many researches. Among these models, artificial neural networks (ANN) and logistic regression (LR) have been so popular (Triantafyllidis and Mountrakis 2012). Logistic regression due to its simple and interpretable structure have been used in this field. On the other hand, ANN due to its fast and parallel processing and also, learning ability for obtaining the expansion patterns, have been used. These popular methods have some disadvantages, too. LR due to its linear structure is unable to deal with the nonlinear parts of the spatial phenomenon. On the other hand, lack of flexibility is one of the ANN disadvantages. Also, ANNs are unable to deal with qualitative uncertainty, too. In this condition, combinations of ANN and Fuzzy Inference Systems (FIS) obviate many of their shortcomings. In other words, by integrating ANNs and fuzzy systems, the capabilities of ANNs self-learning with the linguistic expression function of fuzzy inference can be fused (Pahlavani and Delavar 2014). Dickerson and Kosko (1996), Mitaim and Kosko (2011), Huang and Xing (2002), and Yan (2010) have had such studies that confirm the possibility of extracting fuzzy-rules from training data by integrating fuzzy systems with ANNs. Thus, ANFIS as an ANN based method which takes benefit of fuzzy inference system seems to be appropriate in spatial phenomenon like urban expansion.

Future studies perspective

Asselt et al. (2010), define three different categories of futures studies and how they handle uncertainty, although, different labels are used to categorise futures studies in (Armstrong and Fildes 2006; IPTS-JRC, 2008). Following Asselt et al. (2010), the three proposed categories of future studies include: forecasting, foresight and normative future studies. Forecasting, shows one relatively certain image of the future. The future can be seen as the logical result of the past (Veenman 2013). In fact, Forecasting is a short-, medium- or long-term estimation of future in a specific research area by means of scientific methodology (Cuhls 2003). For this approach, past-based scientific knowledge and models based on these assumptions are considered a reliable basis for making statements about the future (Veenman 2013). In the other words, Forecasting extends past and present patterns and trends into the future, implying a smooth transition between the past, present and the future (Nowotny 2008). Foresight is the second of

Asselt's categories for futures studies that more strongly emphasizes cognitive uncertainty is foresight which deals with multiple possible and plausible future (Veenman 2013). Foresight draws conclusions for the present and is therefore a broad range policy instrument that can serve various objectives (Cuhls 2000). In fact, Foresight is presented in a scenario study as a rich detailed portrait of a plausible future world, or as future states of a system (Berrigi 1997). A scenario is not a forecast but a plausible description of what might occur (Enserink et al. 2010). In foresight studies, future images are given with two or more scenarios (Schwartz 1991; Goodwin and Wright 2010). It is uncertain which trends develop, continue or stop, and which unexpected events might happen, since multiple, alternative futures are possible in foresight analysis (Veenman 2013). Normative, is the third category of future studies of Asselt et al. (2010). In contrast to forecasting and foresight studies, normative futures studies favor normativeness instead of trying to be 'neutral' (Veenman 2013). The normative studies include two branches: backcasting and critical futures studies. Backcasting is concerned with how desirable futures can be created, rather than what futures are likely to occur. In backcasting, one envisions a desired future endpoint, and then works backward to determine what policy measures would be required to achieve such a future. Critical future studies emphasizes that images of possible futures are not neutral but represent particular desires, values, cultural assumptions and world views (Asselt et al. 2010). Such future studies sketch a future that is considered ideal, for example, a situation of peace and tolerance, or a situation where the environmental burden is minimised. These types of future studies do not attempt to imagine one or more possible images of the future or one or more possible images of development without a statement being made about the desirability of it. According to Asselt's category, this paper implemented the first category, forecasting.

Cognition based perspective

Several theoretical perspectives or frameworks have been developed in the study of cognition to organize research, and provide competing and cooperating explanations for cognitive phenomena (Montello and Freundsuh 2005). There are seven major perspectives which provide ample theoretical and conceptual raw material for interpreting past research on cognitive issues in geographic information science, and also, for providing directions for future research (Montello and Freundsuh 2005). They include: constructivism perspective, ecological perspective, information-processing perspective, connectionist perspective, linguistic perspective, situated cognition perspective and evolutionary perspective (Montello and Freundsuh 2005).

In this paper, the research methodology use the information-processing perspective and connectionist perspective categories. Information-processing perspective emphasis on the roles of strategies and metacognition (cognition about cognition) that control the use of cognitive structures when reasoning about particular problems (Montello and Freundschuh 2005). An example is a person using a particular set of rules to perform a GIS procedure on several data layers. The information-processing approach is inspired by traditional rule-based digital computing and is represented by work in formal/computational modeling and symbolic AI. In this study, the data processing section utilized this cognition. For example, Landsat imageries classification in this paper which done using ENVI Software is inspired by information-processing cognition.

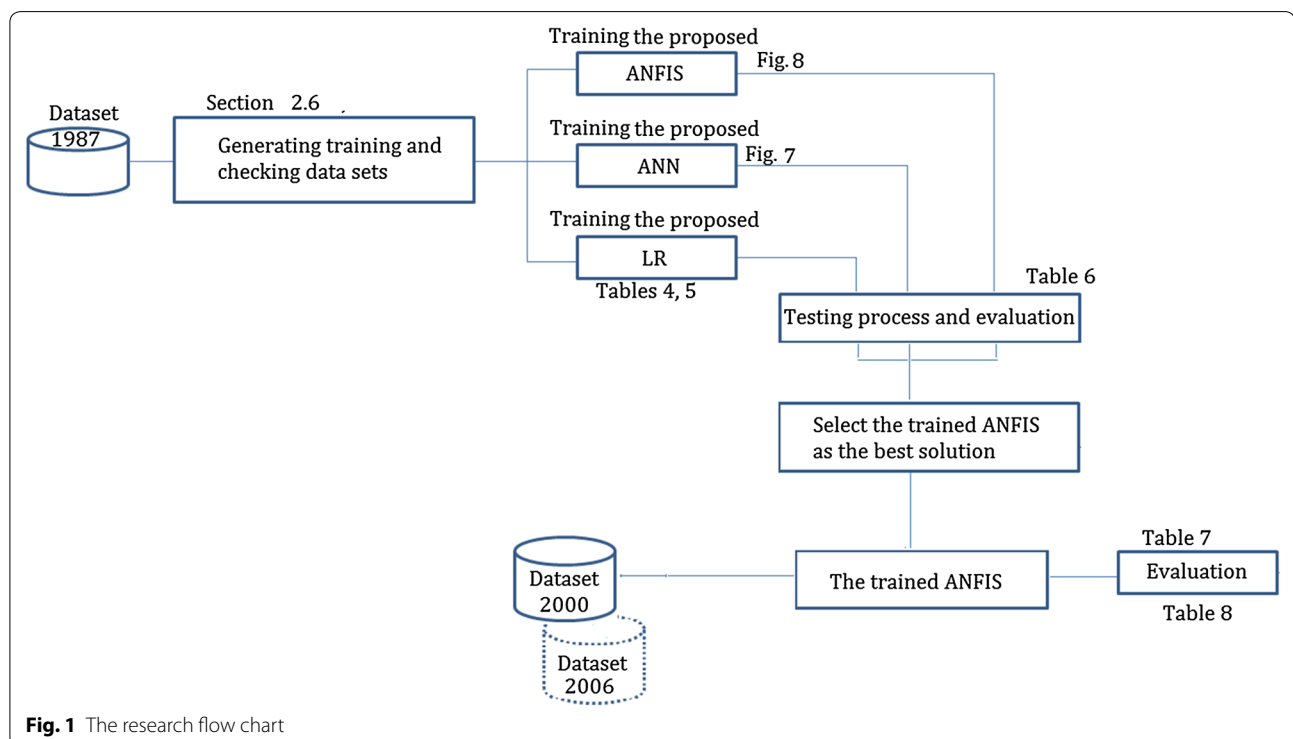
Also, this paper in the modeling section (ANFIS and ANN models) utilized the Connectionist perspective cognition. Connectionist perspective cognition suggests that, cognition operates by the activation of complexly interconnected networks of simple neuron-like nodes. The output of a network is determined by the patterns of interconnecting links, and weights on these links, that affect output from one node to another (Rumelhart and McClelland 1986). It is claimed to be a model of cognition that explicitly ties mental activity to the operation of the brain and nervous system, or at least a neurologically plausible model of the nervous system (Montello and

Freundschuh 2005). Thus, urban growth as a complex system needs different cognition perspectives to be considered in order to model the nature of urban expansion in a better and more accurate way.

In this paper, an ANFIS structure has been proposed for modeling urban land use change and compared its performance with the two popular land use change models, ANN and LR. This paper includes these steps (Fig. 1). The employed dataset including Landsat imageries, road networks and Digital Elevation Model (DEM). Next, we generated training data ("Creating the training data for the LR, ANN and ANFIS models" section) to train the ANFIS, ANN and LR models (Figs. 7, 8; Table 5). The first evaluation step was implemented using comparison between the real training data and the simulated ones using PAM location and quantity (Table 6). Then, the best model was selected and the 2000 and 2006 maps (Figs. 10, 11) simulated and Percent Area Match location and quantity have been used for evaluating the goodness of fit the simulated maps (Tables 7, 8).

Methods

In this section, after introducing the study area ("Study area" section), data pre-processing step ("Data pre-processing" section) and proposed methods ("Artificial neural network specification", "ANFIS specification", "LR" sections), the training data are generated ("Creating the training data for the LR, ANN and ANFIS models"



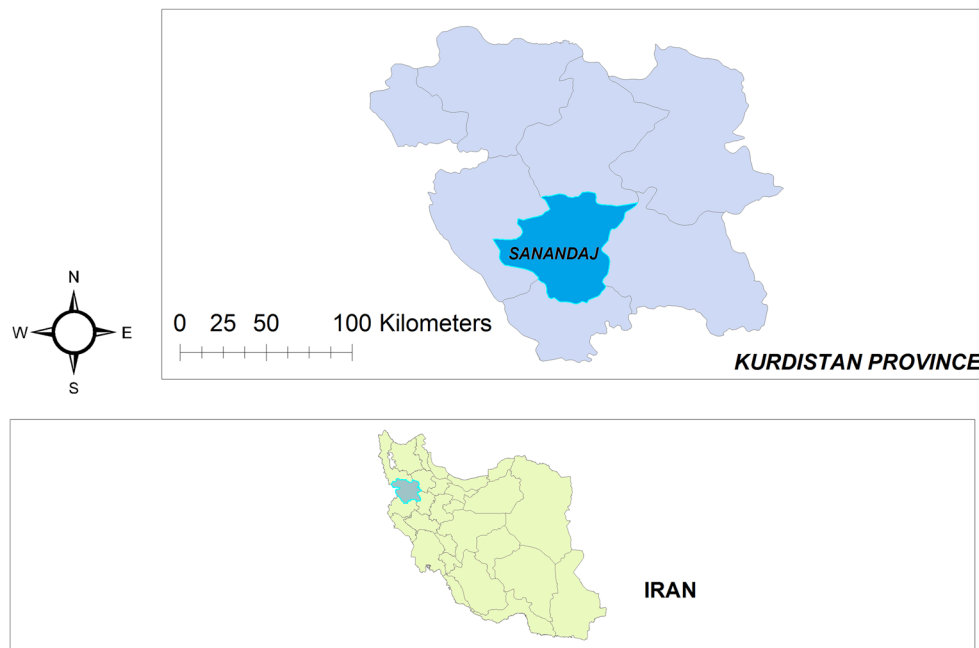


Fig. 2 The study area

section). Then, the three proposed models trained using the training data and PAM quantity and location as the accuracy assessments have been used to determine the best solution between the three proposed models. Then by using the best learned model, we simulated the 2000 and 2006 maps and evaluated the results using the same accuracy assessment factors. Figure 1 presents the flow chart describing the main steps in urban growth modeling.

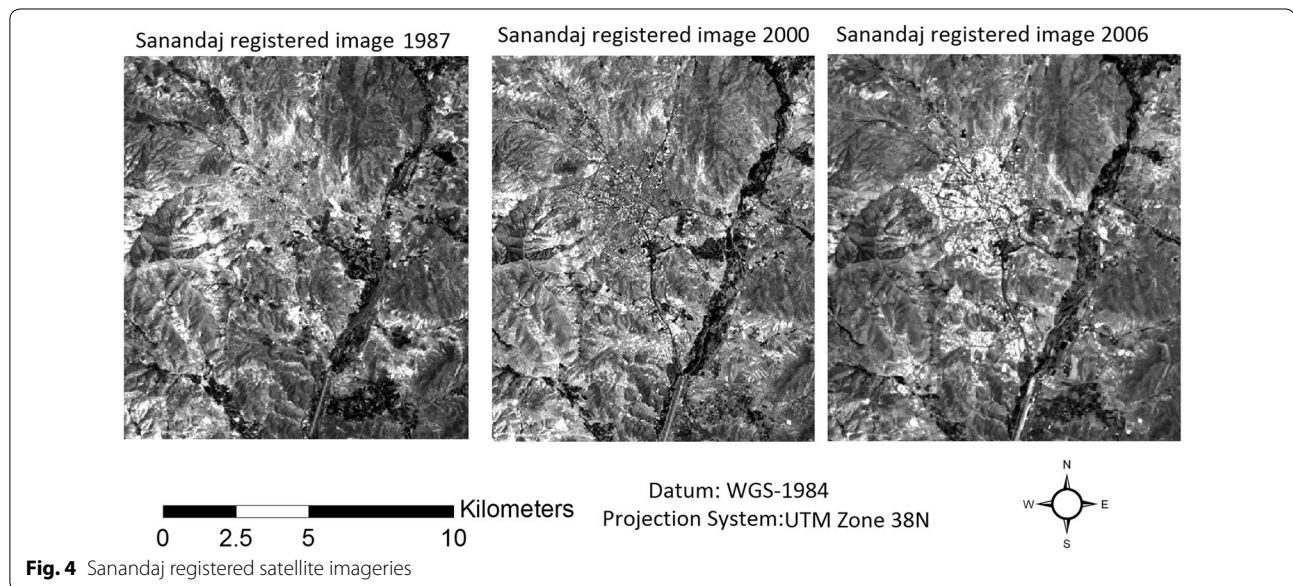
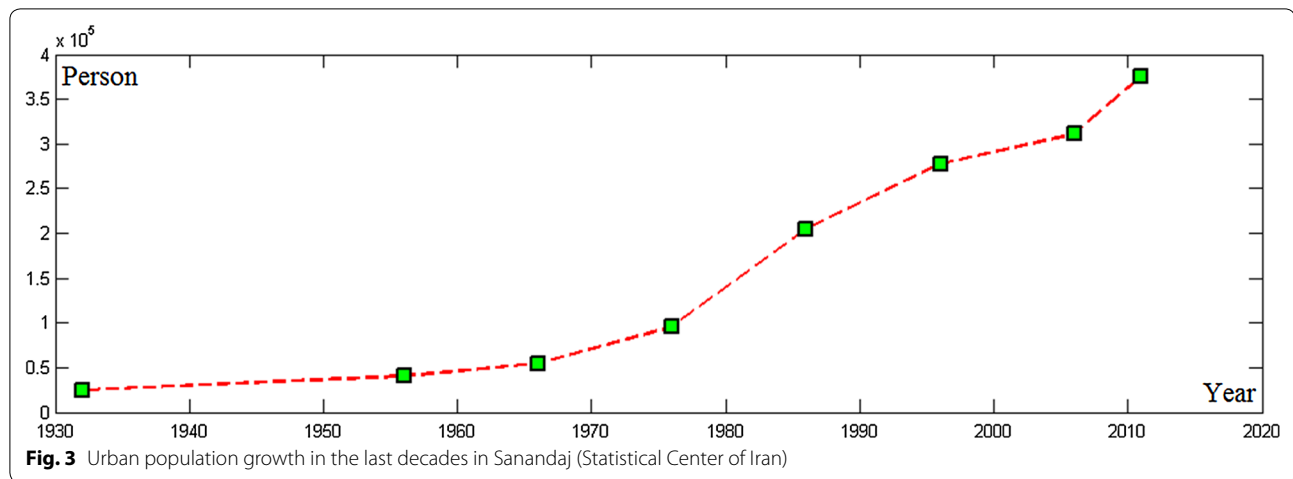
Study area

The study area in this research is the city of Sanandaj in Iran that covers around 3688.6 (ha) with geographical coordinates $35^{\circ} 18' 40''\text{N}$ and $46^{\circ} 59' 40''\text{E}$ (Fig. 2). This city has had a large urban population growth in the last few decades. In overall, socioeconomic processes such as migration, urban sprawl and agricultural developments often contribute to the urbanization. In this city, population growth, migration from neighbourhood cities and even adjacent province to this city are the most important reasons of expanding the city within the last few decades. Figure 3 shows urban population growth in the last decades in this city (Statistical Center of Iran).

Data pre-processing

Nowadays, a plethora of researches in urban management are focused on using GIS, remote sensing and photogrammetric data for simulation modeling of urban growth (Dadras et al. 2015). GIS can be considered as

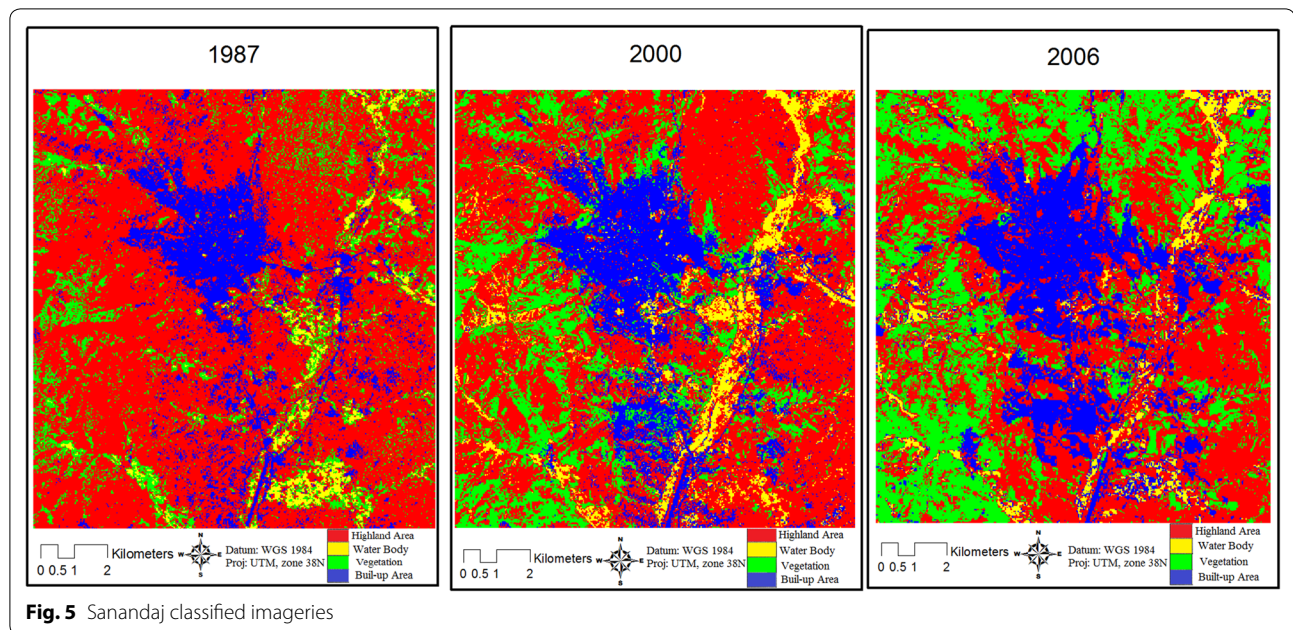
a spatial data management tool which has been used in data pre-process, process and post-process stages. It can be considered as a pre-processor by generating input data derived from a variety of sources; also at each stage of analysis as a data management tool; and finally as a post-processor for data visualization and planning (Kumar et al. 2013). In this condition, remote sensing imageries are a reliable and accurate data sources which are valuable for the analysis and modeling of urban status (Jensen and Cowen 1999; Batty and Howes 2001; Donnay et al. 2001; Herold et al. 2001; Clarke et al. 2002). Temporal frequency, availability of free to less expensive data sources of satellite imagery and image processing techniques have greatly enhanced the potential for monitoring and mapping urban growth and monitoring urban land use change (Goodchild 2000; Im et al. 2008), urban land use dynamics (Herold et al. 2003), landscape pattern analysis (Li and Yeh 2004), and urbanization (Weng 2007). Remote sensing data used in this research, comes from three satellite imageries in 1987, 2000 and 2006 from Landsat TM and ETM⁺ (Fig. 4) with pixel sizes of 28.5 and 30 m, respectively in UTM-WGS 1984 Zone 38 N. The satellite imageries were chosen due to their proper spatial and temporal resolutions presenting different land use policies in Iran in different decades. For the imageries classification, Anderson level 1 due to nature of urban growth (changing from non urban to urban) is considered as the classification scheme and the imageries are classified in four categories including vegetation, developed



area, highland area and water body (Fig. 5). Maximum likelihood classification method has been used for land use/cover classification. Kappa coefficient obtained from the classification, ranges from 89.17 to 92.68 %. According to Pijanowski et al. (2005) and Sousa et al. (2002), all of the obtained Kappa statistics values are considered excellent. Whereas overall accuracy have been obtained equal to 94.27 % for 1987, 92.57 % for 2000, 94.71 % for 2006, respectively. According to Anderson et al. (1976), the obtained overall accuracies are acceptable. Tables 1, 2 and 3 present user and producer's accuracy for 1987, 2000 and 2006 imagery.

The main road map, green spaces and faults are also prepared in GIS environment. Risk assessment factor is an unavoidable factor in urban management. Thus,

considering this factor in the modelling of the city is reasonable. In this research, faults are considered as the area which has the potential of danger. Thus, distance to this dangerous area is another factor which has been considered in the dataset. The developed area and city center layers are obtained from the classified images. The distances to the developed area, green spaces, roads, city center, faults and also, number of urban cells in a 3 by 3 kernel are obtained in Matlab. The slope and elevation layers are from AsterDEM data. The final dataset includes distance to main road, distance to green spaces, distance to faults, distance to developed area, slope, elevation, distance to district centers and number of developed cell in a 3 by 3 neighbourhood (Fig. 6).


Table 1 Classification accuracy (1987)

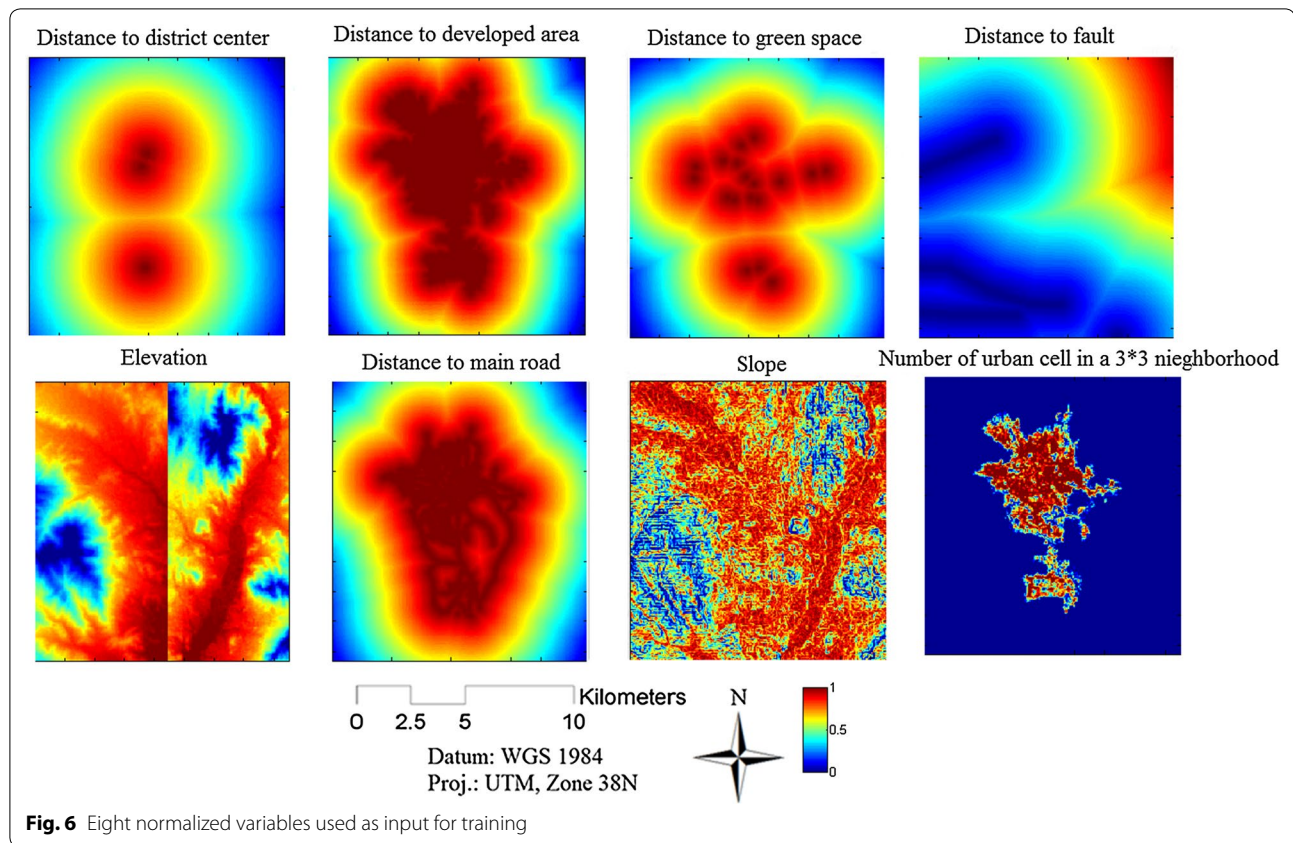
Class name	Reference totals	Classified totals	Number correct	Producer's accuracy	User's accuracy
Water body	27	28	26	96.30	92.86
Built-up area	38	49	38	100	77.55
Highland area	155	149	144	92.90	96.64
Vegetation	89	83	83	93.26	100.00
Total	309	309	291		

Table 2 Classification accuracy (2000)

Class name	Reference totals	Classified totals	Number correct	Producer's accuracy	User's accuracy
Water body	123	120	120	97.56	100
Built-up area	177	219	173	97.74	79
Highland area	505	483	455	90.10	94.20
Vegetation	286	269	262	91.61	97.40
Total	1091	1091	1010		

Table 3 Classification accuracy (2006)

Class name	Reference totals	Classified totals	Number correct	Producer's accuracy	User's accuracy
Water body	118	147	117	99.15	79.59
Built-up area	176	177	175	99.43	98.87
Highland area	243	214	213	87.65	99.53
Vegetation	87	86	86	98.85	100
Total	624	624	591		



Artificial neural network specification

According to the recent researches, data driven inductive methods are popular. Because first, they have been extracted from the data and relation between them. Second, they tend to perform better in reproducing existing spatial patterns (Overmars et al. 2007; Koomen et al. 2015). Artificial neural networks with capacity of nonlinear, parallel and highly complex processing have been employed in many fields such as climate forecasting (Panagoulia 2006), agricultural land suitability assessment (Wang 1994), remote sensing (Morris et al. 2005) and land use change and urban growth modeling (Tayyebi et al. 2011; Pijanowski et al. 2002, 2009, 2014). Artificial neural network is a powerful tool in environmental modeling (Li and Yeh 2001). The ability to learn is the most important feature of this method. In the other words, the network uses data to identify patterns and relationships among the data. According to Almeida et al. (2008), Li and Yeh (2002), ANN method has the ability to capture the non-linear relationships presented in many geographic phenomena (Li and Yeh 2002; Li et al. 2003). Thus, it can be used due to this ability to compute the conversion probabilities for competing multiple land uses. There is a general consensus among researchers in the field of urban modeling that empiricism is a

reasonable way to determine the most optimum and the best structure in neural net for a specific problem (Li and Yeh 2001; Yeh and Li 2003; Guan and Wang 2005; Almeida et al. 2008). Also, there is no certain rule for determining optimum number of hidden layer and also neurons in the hidden and output layers. In this study, an ANN structure with three layers has been used. The input layer includes eight neurons. Also, The output layer includes two neurons which is the number of classes (urban and non-urban). Tangent sigmoid in the hidden layer and (Purelin) linear function as the transfer function in the output layer have been used.

ANFIS specification

ANFIS was introduced first by Jang (1993). This method is developed through the integration of ANN and fuzzy logic models which enables us to integrate learning capability and human knowledge together in one method and at the same time to cover many of their shortcomings such as lack of flexibility in ANN and finding out the correct positions and shapes for membership functions in FIS (Mohammady et al. 2013). In this algorithm, during the learning process, membership functions in fuzzy structures change toward their optimal values (Mohammady et al. 2013). In this paper, an ANFIS structure

which generated a Sugeno-type Fuzzy Inference System (FIS) structure using subtractive clustering method has been used. The subtractive clustering method has been chosen as the generating FIS method, because of high dimension of the input data. The rule extraction method first uses the subtractive clustering function to determine the number of rules and antecedent membership function and then, uses linear least squares estimation to determine each rules consequent equation (Chiu 1994). Gaussian membership function as the input membership function has been used. Since the dataset has 8 input variables and 1 output variable, sub cluster constructs a FIS with 8 inputs and 1 output. In this method, sub clustering identifies the number of membership function for each input and output which is as many as the number of clusters (Chiu 1994).

LR

Logistic regression method was proposed by Christensen (1997). This method is one of the most popular methods for urban growth modeling (Triantakou and Mountrakis 2012). Linear regression explores the relationships between independent variables and urban land uses. In this field, the dichotomous dependent variable is urban change, where a value of 1 indicates change from non-urban to urban and 0 indicates no change. According to Christensen (1997), the probability of each ground pixel to being developed to an urban land is considered by [Eq. (1)]

$$P = \frac{\exp(B_0 + \sum_{i=1}^n B_i X_i)}{1 + \exp(B_0 + \sum_{i=1}^n B_i X_i)} \quad (1)$$

where, P is the probability of land use change for each cell, X_i is the effective parameters in urban growth, B_0 is the constant parameter, B_i is the coefficients of each of the independent parameters that must be calculated. P indicates the probability of change from non-urban to urban. The output of the P is always a value between 0 and 1.

Creating the training data for the LR, ANN and ANFIS models

The selection of training dataset size for ANNs should be done carefully, because ANNs have the tendency to overfit data (Huang and Huang 1991). According to the proposed activation functions in each method, all of the input values converted to -1.0 to 1.0 range for the ANN model and between 0 and 1 for ANFIS and LR. Normalization function which is used for projecting the data between 0 and 1 (ANFIS and LR) is shown in [Eq. (2)] and [Eq. (3)] for ANN structure.

$$x'_j = \frac{x_j - \min(x_j)}{\max(x_j) - \min(x_j)} \quad (2)$$

$$x'_j = 2 * \left(\frac{x_j - \min(x_j)}{\max(x_j) - \min(x_j)} - 0.5 \right) \quad (3)$$

$$(x_1, x_2, \dots, x_n), \quad n \in (1, 2, 3, \dots, 8)$$

$$(x'_1, x'_2, \dots, x'_n), \quad n \in (1, 2, 3, \dots, 8),$$

where, x_j : real value for each input data and x'_j : normalized value for each input data.

The final matrix which is prepared to enter ANFIS structure is shown as follows:

$$Data = \begin{pmatrix} x'_{11} & x'_{12} & x'_{13} & \dots & x'_{18} & 1 \\ & \vdots & & \ddots & & \vdots \\ x'_{n1} & x'_{n2} & x'_{n3} & \dots & x'_{n8} & 1 \\ x'_{n+11} & x'_{n+12} & x'_{n+13} & \dots & x'_{n+18} & 0 \\ & \vdots & & \ddots & & \vdots \\ x'_{n+m1} & x'_{n+m2} & x'_{n+m3} & \dots & x'_{n+m8} & 0 \end{pmatrix}$$

$i = 1, 2, 3, \dots, n, n+1, n+2, n+m$ and $n+m = \text{number of samples } j = 1, 2, 3, \dots, 8 \text{ (input index)}$

In this matrix, columns 1–8 are the input data and the last column indicates value of the cell obtained from the observed data of urban change. The value of 1 in the last column indicates that a non-urban cell changed to urban and 0 indicates no change to urban. RMSE values are generated for each cycle. Then, the RMSE values are plotted against the number of training cycles (epochs) to identify the best fitting model.

Results

Models calibration

The training data in this study area includes 25 % (50,000 cells) of all the data, which 36 % of these training data (18,000 cells) were entered (ANFIS, ANN and LR) to train and estimate the bias and the rest 64 % (32,000 cells) were used as the data check. The training data (50,000 cells) were 25 % of the 1987 image data which have been used for calibrating the models as training and checking for ANN and ANFIS models and calculating LR parameters. The training data have been chosen from all the image area in a random manner which guarantees there is no bias in the selection. Then, after the selection of the sample data, the models are calibrated.

In this research, the nets have been trained until reaching a stable situation. As it is presented in Fig. 7, the ANN error curve (RMSE) for training data starts around 1.1 and reached under 0.4 after 1500 epochs. The ANN error curve for checking data starts around 1.25 and after 1500 epochs reached around 0.9.

For the ANFIS, Gaussian membership function with 0.1 as the initial step size is used. The step size decreasing and increasing rates were selected equal to 0.9 and

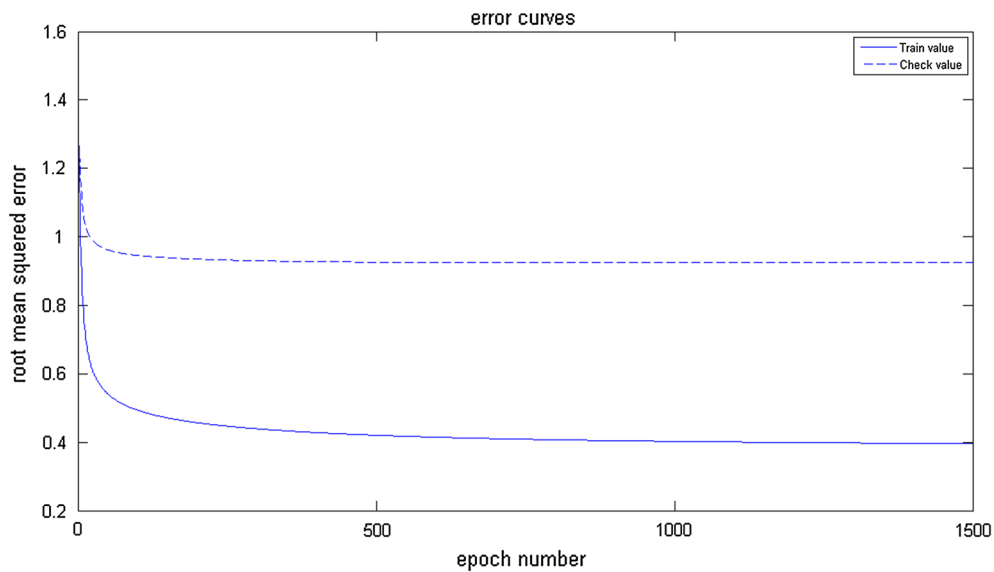


Fig. 7 ANN error curves

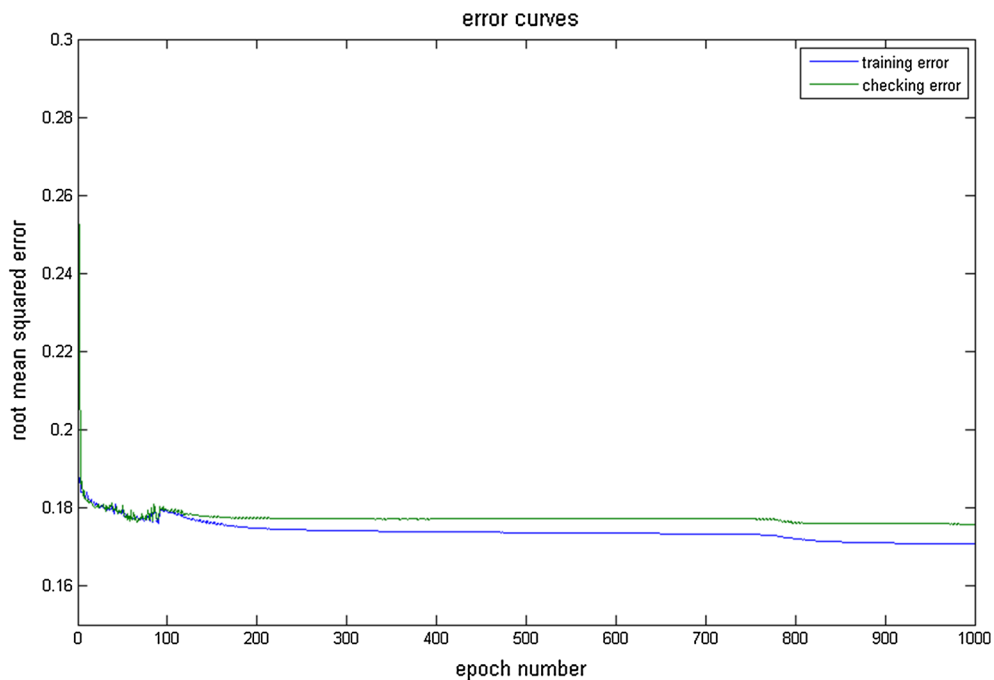


Fig. 8 ANFIS error curves

1.1, respectively. This method selects the number of membership functions from the input data. Figure 8 illustrates training run of ANFIS which RMSE was plotted across training cycles. The ANFIS error curve for training data and checking data starts around 0.19 and 0.25, respectively. After 200 epochs, both of the curves missed their oscillation and have changed very smoothly toward their final values in epoch 1000 to

around 0.17 for both of the training and checking data. The input and final membership functions are illustrated in Fig. 9.

The correlation between the input parameters is shown in Table 4. According to Table 4, correlation between neither of the pair input parameters have been more than 0.5 and this means the input parameters in this research have been independent. The LR calibrated results are

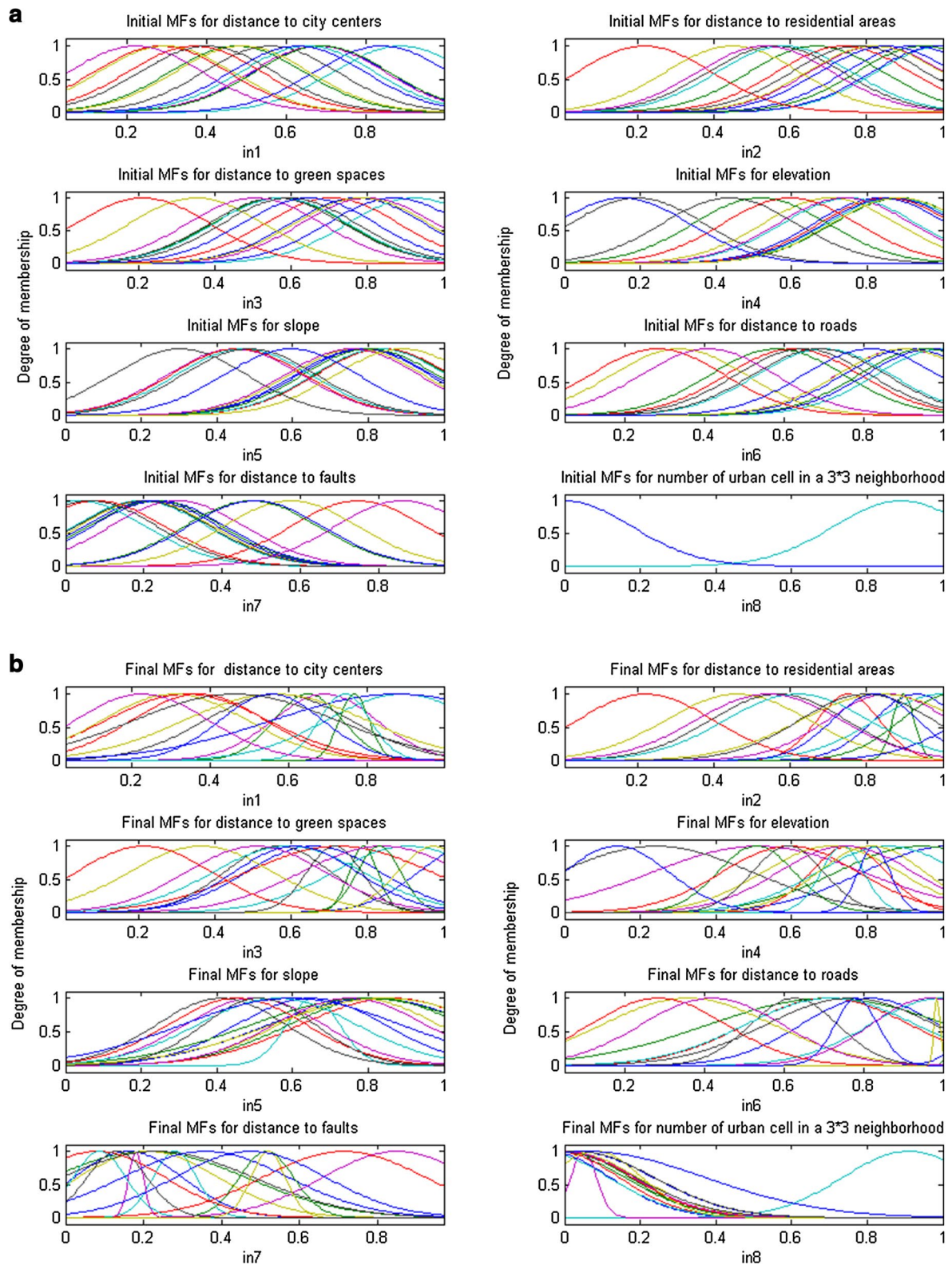


Fig. 9 **a** Initial membership functions. **b** Final (optimized) membership functions

Table 4 LR correlation matrix

Inputs variable								
Distance to region centers	1	0.131	−0.325	−0.119	0.033	−0.285	0.336	−0.082
Distance to developed area		1	−0.097	0.108	−0.131	−0.138	−0.043	−0.431
Distance to green space			1	−0.161	−0.008	−0.464	−0.142	0.118
Elevation				1	−0.255	0.084	0.315	−0.009
Slope					1	0.030	0.088	−0.036
Distance to main road						1	−0.158	0.011
Distance to fault							1	0.055
Number of urban cell in a 3*3 neighborhood								1

shown in Table 5. According to Table 5, the distance to the developed areas and the distance to main roads are the most important drivers in growth of this city during 1987–2006. On the other hand, the slope and distance to the faults were the ones which had the least impact on Sanandaj urban growth.

Accuracy assessment

In this paper, Percent Area Match (PAM) metrics have been used to evaluate each model. PAM compares areas that are correctly predicted as change according to the model compared with areas that are converted to new areas in the observed map. PAM quantity [Eq. (4)] and location [Eq. (5)] are important for urban planners because it is vital for them to know the spatial location and quantity of land area within the urban boundary around the urban area. Values less than 1, indicates that the model underestimates the size of the urban area and

values greater than 1, reflects that the model overestimates urban area (Tayyebi et al. 2011).

$$PAM \text{ quantity} = \frac{APt_2 - AAt_1}{AA_t2 - AAt_1} \quad (4)$$

$$PAM \text{ location} = \frac{(APt_2 - AAt_1) - \alpha}{AA_t2 - AAt_1} \quad (5)$$

$$\alpha = \frac{APt_2 - AAt_2}{AA_t2} \quad (6)$$

where, AAt_1 is the area within actual urban boundary in time 1, AA_t2 is the area within actual urban boundary in time 2, APt_2 is the area within predicted urban boundary in time 2.

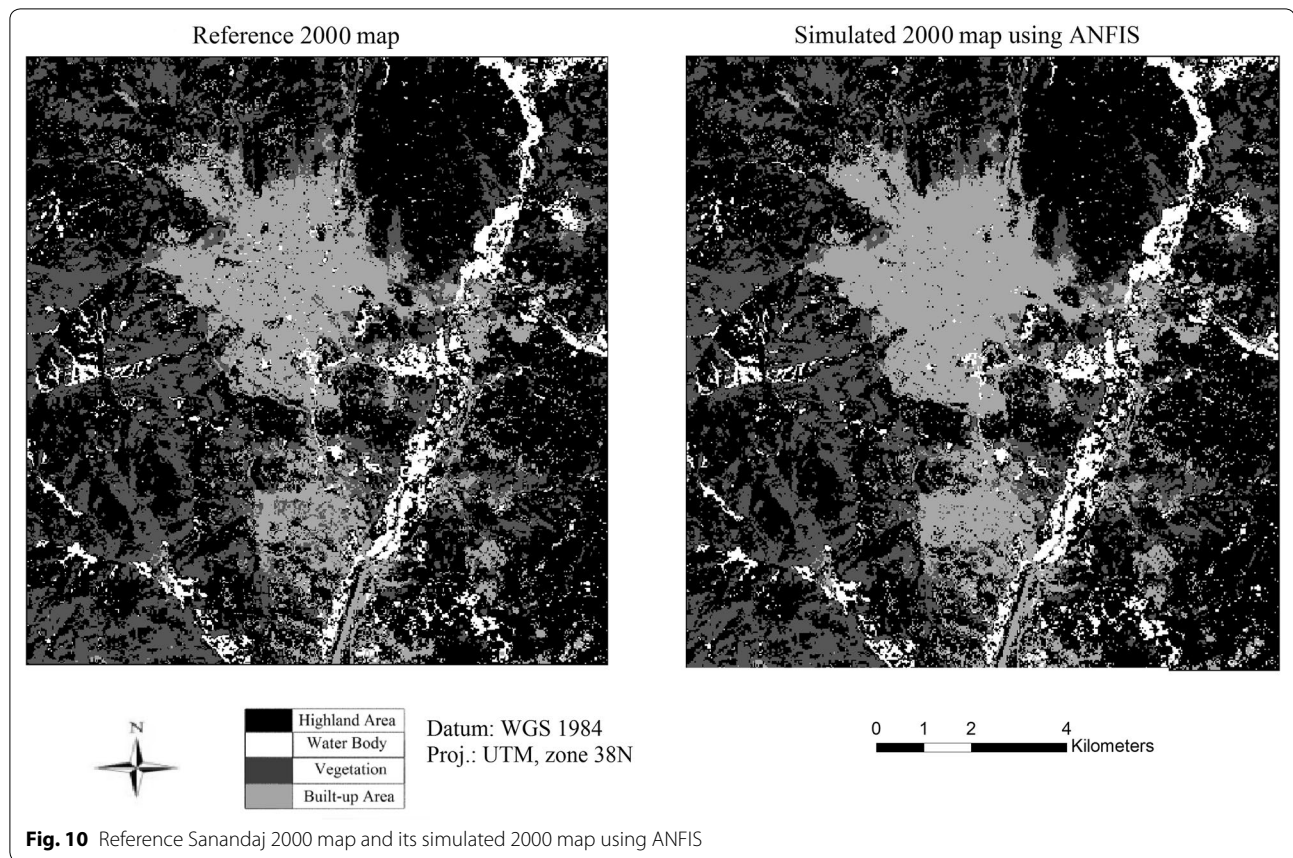
Table 6 show the goodness of fit resulted from the training and checking data for all the three models. In this step, the best solution which has the best goodness

Table 5 LR parameters

Input variable	Coefficient	Standard error	Exp. (coefficient)
Distance to region centers	6.347	0.416	570.687
Distance to developed area	19.496	0.973	2.932E8
Distance to green space	−0.759	0.450	0.468
Elevation	1.196	0.206	3.305
Slope	−0.029	0.170	0.972
Distance to main road	10.013	0.959	2.232E4
Distance to fault	−0.315	0.244	0.730
Number of urban cell in a 3*3 neighborhood	3.429	0.121	30.848
Constant	−34.935	1.100	0.000

Table 6 Simulation results for 2000 map with training and check data using ANFIS, ANN and LR

Method	Area in 1987 (km ²)	Area in 2000 (km ²)	Predicted area in 2000 (km ²)	PAM quantity	PAM location	Situation
ANFIS	2.9720	4.8580	4.8848	1.0142	1.0113	Overestimate
ANN	2.9720	4.8580	4.8995	1.022	1.0174	Overestimate
LR	2.9720	4.8580	4.9182	1.0319	1.0253	Overestimate



of fit is selected as a final method for modeling urban growth of the 2000 and 2006 maps. According to Table 6, the ANFIS model has had the best goodness of fit among the three models. Thus, this model is used for modeling urban growth in 1987–2000 and 2000–2006. Figures 10 and 11 show the results of the Sanandaj growth simulation for 2000 and 2006 respectively using ANFIS model (the best model). Tables 7 and 8, show the results of implementing the ANFIS model for modeling urban growth for 2000 and 2006.

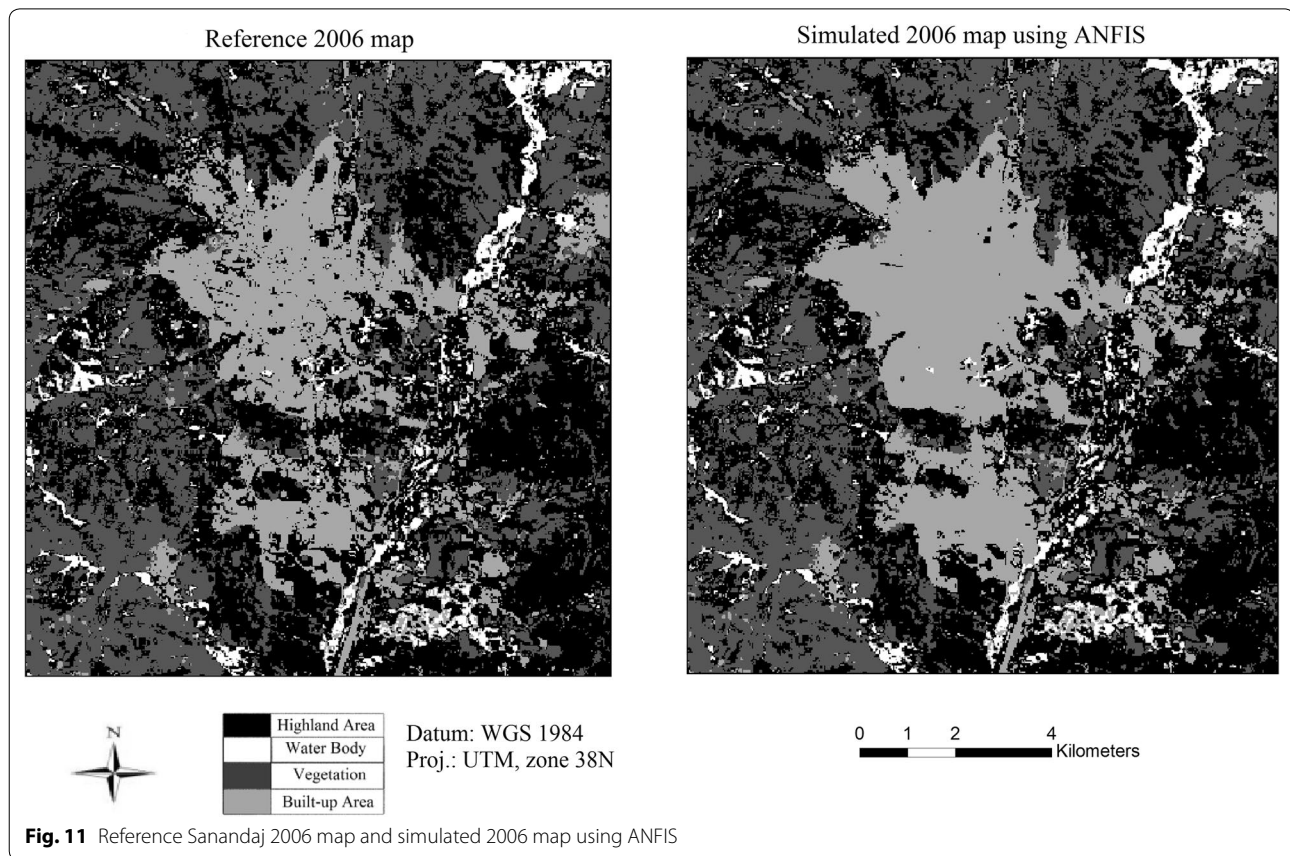
Discussion

In Sanandaj city during the 1987–2006, the most significant growth has occurred in the southern part of the city. Although, in the north, east and west of city, urban growth has been occurred. However, exiting of the high elevation areas in the west, southwest, north and northeast played as a burrier role in the development of these regions. In addition, the areas in the south west have experienced more growth, as these areas are well served by the urban road network and had appropriate elevation and slope situation.

According to Table 5, distance to developed areas and distance to main roads due to their high values have been the most important factors in the expansion of Sanandaj city during 1987–2006. On the other side, slope and distance to fault had the least impact in expansion of the city due to their small values.

According to Table 6, the ANFIS model has the best goodness of fit among the three models. The predicted urban areas for 2000 map using training and checking data in ANFIS method has been so close to the real urban area for 2000 map than ANN and LR results. Also, the predicted urban area using ANFIS model for 2000 and 2006 maps (Tables 7, 8) have created PAM location and quantity values close to 1 which means the predicted area in both 2000 and 2006 maps have had acceptable agreement with the real ones.

As observed from the existing growth trends until 2006, urban growth policies have not paid serious attention to risk assessments factor such as distance to faults in development of the city which can be a major challenge at high dense urban areas.

**Table 7** Simulation results for 2000 map (testing data) using ANFIS

Method	Area in 1987 (km ²)	Area in 2000 (km ²)	Predicted area in 2000 (km ²)	PAM quantity	PAM location	Situation
ANFIS	9.2076	15.1963	15.2436	1.0079	1.0073	Overestimate

Table 8 Simulation results for 2006 map using ANFIS

Method	Area in 2000 (km ²)	Area in 2006 (km ²)	Predicted area in 2006 (km ²)	PAM quantity	PAM location	Situation
ANFIS	17.7647	22.4977	22.6387	1.0298	1.0288	Overestimate

Linguistic knowledge through fuzzy inference system can easily be used to model the urban development. So, knowledge and uncertainty about urban development can be easily incorporated into the modeling process. Needless to say that urban planners and urban managers need to provide rules or knowledge instead of exact mathematic expressions for spatial phenomena (Al-Kheder et al. 2008).

The results of research using ANFIS approach have had better goodness of fit than those of ANN and LR

approaches in modeling urban growth for Sanandaj city.

Conclusion

Recently, in Iran, policy makers and urban planners and managers have begun to use urban growth models, both locally and nationally and policies related to land use and urban growth to support efficient use of land and natural resources (Tayyebi et al. 2011). So, urban growth models are powerful tools for urban planners and decision

makers to manage and analyse directions and volumes of expansion of cities.

Combination of remote sensing data, geospatial information systems and artificial intelligence can be a powerful and useful method to analyse and model environmental phenomena such as urban growth. This combination has the potential to support such models by providing data and analytical tools for the study of urban planning. In fact, GIS and RS are considered as new reliable ways providing the necessary information and intelligence for planning proposals and can be used as monitoring tools during the implementation of plans.

The result of using more membership functions in ANFIS algorithm is that more accuracy can be achieved in the fewer epochs. On the other hand, use of more membership functions means that the network architecture needs more memory and also more time to reach the predefined error threshold value.

Neither of the considered methods, has limitation on the input data, evaluation and sensitive analysis consideration. They support all kind of input data such as socioeconomic and biophysical data. In a number of commonly used methods such as SLEUTH, the method cannot support socioeconomic data such as population. In addition, in the software based methods like SLEUTH, there is no way for considering sensitive analysis. Increasing the number of input parameters in ANFIS structure could be done with the least change in structure and program. Like other method with an ANN component, in ANFIS the weights and bias of each neuron could not be elaborate separately. This issue is one of the most important ANN's drawbacks. Thus, in this aspect LR model is simple, clear and has an interpretable structure that could easily determine the weights and importance of each input.

In this study, ANFIS model had the benefits of using neural networks and fuzzy logic at the same time. It was able to identify important factors in the development and their relationship and influence on the growth of the city.

Uncertainty is an indispensable component of spatial phenomena. Urban expansion due to its spatio-temporal nature has greatly affected by uncertainty. ANFIS includes fuzzy inference which is able to deal with uncertainty.

Due to LR model's simplicity and fast processing capability, it is a well-known method in urban growth and land use change modeling. However, it should be mentioned that this method is unable to model the nonlinear parts of the land use change phenomenon and the huge difference between the result of LR and ANFIS may be due to their structures. On the other hand, ANFIS is a well-known method in nonlinear problems, therefore;

it has this ability to deal with complex problems such as urban growth.

Dealing with large data set is a traditional issue in environmental modeling like urban growth and land use change modeling. One of the solutions for the future researches could be clustering the input data and selecting the important ones to make the processing time shorter.

Using satellite imageries with high spatial resolution such as IKONOS, Quickbird and Orbview may enhance the classification accuracies. In this study, three Landsat imageries acquired at 1987, 2000 and 2006 have been used. But it should be mentioned that for a developing country like Iran which historical urban data and land use map is not stored properly or even existed, this research using free and reliable satellite imageries data which is the single source of data for these regions is a practical and scientific method for analyzing urban growth.

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